

## Guest Editorial

# Recent Advances in Capacity Approaching Codes

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SINCE the “turbo revolution” of 1993 and the “rediscovery” of low-density parity-check (LDPC) codes shortly thereafter, the world of channel coding has undergone a major transformation. The “conventional wisdom” of the 1960s, 1970s, and 1980s was that, although capacity was theoretically achievable, practical constraints typically limited the performance of implementable code designs to fall several decibels short of capacity. This understanding was shattered with the invention of turbo codes, which achieved performance roughly 0.5 dB from capacity with moderately complex iterative BCJR decoding, and within just a few years, capacity approaching schemes using LDPC codes along with linear (in block length) complexity message passing decoding were becoming commonplace.

Past issues of JSAC have been in the forefront of keeping the research community current with the latest trends in capacity approaching codes. In February 1998, JSAC published *Concatenated Coding Techniques and Iterative Decoding: Sailing Towards Channel Capacity*, edited by S. Benedetto, D. Divsalar, and J. Hagenauer. The issue contained 16 papers, all of which dealt with some aspect of turbo codes. Then in May and September of 2001, JSAC published *The Turbo Principle: From Theory to Practice I* and *The Turbo Principle: From Theory to Practice II*, edited by P. Siegel, D. Divsalar, E. Eleftheriou, J. Hagenauer, and D. Rowitch. Part I contained 17 papers, 14 devoted to various types of turbo codes, and 3 on LDPC codes. Part II contained 15 additional papers related to applications of the turbo principle in other areas of communication theory. Then in August 2009, JSAC published

*Capacity Approaching Codes*, edited by D. Costello, S. Lin, T. Richardson, B. Ryan, R. Urbanke, and R. Wesel. A total of 18 papers were published, 11 on LDPC codes, 4 on turbo codes, and 3 on other coding-related topics, indicating a clear shift in the interests of the research community toward LDPC codes.

The current JSAC special issue reflects a further shift of interest in coding theory research, this time toward polar codes, a new class of *capacity achieving* codes introduced in 2008. Of the 17 papers appearing in this issue, 9 are devoted to various aspects of polar codes, with 6 papers devoted to LDPC codes, including 3 on spatially coupled (convolutional) LDPC codes, and 2 on other coding topics. Below we give a brief summary of each paper, starting with the papers on polar codes.

### I. POLAR CODES

The issue begins with an historical overview paper by E. Arıkan on the origins of polar coding. It starts by reviewing the role that the channel cut-off rate  $R_0$ , sequential decoding of convolutional codes, and the successive-cancellation framework played in the development of polar codes and concludes by explaining the polar coding concept from this perspective. Of particular interest is the notion that polar codes were originally intended to be the inner code in a concatenation scheme with a convolutional outer code paired with sequential decoding. However, the polar coding concept by itself turned out to be so powerful that no outer code was needed.

The eight other papers on polar codes investigate various aspects of polar code design, decoding techniques, and extensions. The paper by Renes *et al.* deals with the *alignment* of polarized codes and how this relates to the notion of *universality*. Two conditions are derived, one for alignment and one for nonalignment, and the set of channels for which alignment occurs, implying universality, is expanded compared to what was previously known.

The paper by Presman *et al.* introduces a novel construction for polar codes, called a *mixed-kernel* construction, based on code decomposition. Channel polarization is proven for the new construction, and mixed-kernal polar codes are shown to have performance and decoding complexity advantages in the finite block length regime.

The paper by Trifonov and Miloslavskaya introduces the concept of *dynamic frozen bits* and shows how these can be used to describe certain *subcodes* of an arbitrary linear block code as polar codes. This allows larger minimum distances to be achieved, thereby improving the finite block length scaling behavior.

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The paper by Wang *et al.* considers the serial concatenation of an inner polar code with outer BCH and convolutional codes, a combination suggested in the overview paper by Arikan. The major result is to demonstrate that this combination provides an efficient tradeoff between error-correction performance and decoding complexity.

The paper by Wei and Ulukus presents a polar coding scheme that achieves the information-theoretic capacity of the *general wiretap channel* and applies the results to a number of *multiuser channels* to achieve their best-known inner bounds. As such, the polar coding approach serves as a bridge between recent results in information-theoretic security and emerging applications in wireless communications.

The paper by Zhang *et al.* proposes a modified low complexity *successive cancellation list* (SCL) decoder for polar codes that relies on the idea that path splitting may be unnecessary when the reliability of an unfrozen bit is sufficiently high. The modified SCL decoder is shown to achieve a significant reduction in decoding time with only a slight penalty in error-correction performance compared to a conventional SCL decoder.

The paper by Fan *et al.* pursues a related concept called *selective expansion* along with a *double thresholding* list-sorting algorithm to reduce the latency of SCL decoding implementations of polar codes. A VLSI implementation using CMOS technology is then used to demonstrate that the resulting penalty in error-correction performance is negligible.

Finally, the paper by Sarkis *et al.* also deals with SCL decoder implementations for polar codes. In particular, software implementations of fast SCL decoders, which make use of a method of *unrolling* the decoding tree to improve speed, are demonstrated and compared. An application to software-defined radio is also included.

## II. SPATIALLY COUPLED CODES

The paper by Liu *et al.* introduces a new algebraic construction method for *spatially coupled* (convolutional) LDPC (SC-LDPC) codes, called *replicate-and-mask* (R&M). The R&M method, which has been previously employed to construct good *quasi-cyclic* LDPC block codes, is extended to construct quasi-cyclic SC-LDPC codes with guaranteed girth, and the new codes are compared to conventional quasi-cyclic SC-LDPC codes obtained using the unwrapping method.

The paper by Stinner and Olmos analyzes the *finite-length scaling* behavior on the binary erasure channel (BEC) of structured SC-LDPC codes constructed using *protographs*, thus extending previous work by the second author for random code ensembles. The results indicate that the additional structure imposed by protograph-based ensembles improves the finite-length scaling performance.

The paper by Huang and Ma is devoted to a performance analysis of *Block Markov Superposition Transmission* (BMST) codes, a type of serially concatenated code with easy encoding that uses short block codes as component codes. The encoding method is shown to be equivalent to *spatial coupling* of the generator matrix, and performance comparisons to SC-LDPC codes and ARJA-type LDPC block codes indicate excellent waterfall region behavior.

## III. LDPC CODES

The paper by Ganesan *et al.* investigates the important practical problem of determining the total power, including both *transmit power* and *decoding power*, needed to guarantee a certain hard-decision iterative decoding error probability for a class of LDPC codes operating on the AWGN channel. Two models of decoding power are considered, where all the power is consumed either by the processing nodes or by the wires, and analytical bounds are obtained in each case.

The paper by Steiner *et al.* considers the joint optimization of protograph-based LDPC code ensembles and bit mapping for shaped bandwidth-efficient bit interleaved coded modulation (BICM) on the AWGN channel. *Constellation shaping* and *bit-level reliabilities* are taken into account in the optimization, and ensembles are found that outperform the best currently known designs for bandwidth-efficient coded modulation with shaping.

The paper by Mitchell *et al.* investigates the iterative decoding thresholds of high-rate LDPC code ensembles derived from a lower rate mother code ensemble by *random puncturing*. In particular, it is shown that the BEC and AWGN thresholds of randomly punctured LDPC code ensembles can be accurately predicted using a single constant, which depends only on their design rate and the BEC threshold of the mother code ensemble.

## IV. CODING THEORY

The paper by Lazaro *et al.* analyzes the minimum distance properties of *fixed-rate raptor codes* with linear random codes as outer codes. The *average weight enumerator* is formulated and necessary and sufficient conditions for fixed-rate raptor code ensembles to achieve *linear minimum distance growth* are derived, where the weight enumerator and the distance growth rate are expressed as functions of the rate of the outer code and the degree distribution of the inner LT code.

## V. CODING APPLICATIONS

The paper by Zeineddine and Mansour presents a two-step coding scheme for application to time-varying channels in wireless broadcast communications. In the proposed scheme, frames are encoded individually and then a second layer of *interframe* coding is applied across frames. This structure leads to an *iterative rate-matching decoding* process, which is shown to result in a better complexity versus data-rate tradeoff than previously existing approaches.

## VI. SUMMARY

This special issue captures a snapshot of the continuing evolution of research interests in the fascinating area of capacity approaching codes. Once it was understood by researchers that it was possible to implement practical coding schemes with near-capacity performance, the digital communications and data storage industries, along with the associated standards committees, quickly took note of the new methods. Turbo codes were adopted for several coding standards in the late 1990s, shortly followed by LDPC coding standards in the 2000s. Now, reflecting the shift in research interests noted in this special

issue, both polar codes and spatially coupled LDPC codes are being actively considered for future coding standards. This activity underscores the remarkable staying power of channel coding theory as a research topic of great theoretical and practical interest over a span of time that now exceeds 60 years.

#### ACKNOWLEDGMENT

We would like to thank all the authors who submitted their research papers to the special issue. We particularly appreciate their efforts to submit their materials in a timely manner. The overall quality of the submissions was very high, and we regret that, due to space and time constraints, we could not have accepted more papers. Special thanks are also due to the reviewers, who were very responsive to our repeated reminders about staying on schedule. Their critical comments and suggestions to the authors contributed greatly to the final product. We are also thankful to M. Medard, JSAC Editor-in-Chief, Executive Editor L. Greenidge, and Editorial Assistant L. Briede at IEEE Publishing Operations for the co-operation and encouragement they have provided to this project. Finally, thanks are due to the JSAC Editorial Board Representative M. Pursley for suggesting to us that “it might be time for another special issue on coding” and for presiding over the guest editor submissions.



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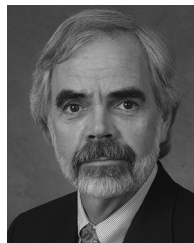


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